

**EXPERIMENTAL AND NUMERICAL
ESTIMATION OF DAMPING
IN COMPOSITE PLATES WITH
EMBEDDED VISCOELASTIC
TREATMENTS**



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...to my loving parents and my wife Fiorenza

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